

Similar to Binary tree except that the elements to the left side of any node must be smaller than the node (parent) and the elements to the right must be greater or equal to the parent node value

```
#include <stdio.h>
#include <stdlib.h>
```

```
struct tree
{
    struct tree *left;
    char data;
    struct tree *right;
} * root = NULL;
```

```
void insert(struct tree *temp, struct tree *nn)
{
    char ch;

    if (nn->data < temp->data)
    {
        if (temp->left == NULL)
            temp->left = nn;
        else
            temp->insert(temp->left, nn);
    }
}
```

II - Binary
insertion

```
if (temp->right == NULL)
    temp->right = nn;
else
    insert(temp->right, nn);
}
```

```
} // end of insert function.
```

```
void create()
```

```
{
```

```
    struct tree *nn;
```

```
    char ch; char x;
```

```
    do
```

```
    {
```

```
        printf("Enter data");
```

```
        x = getch();
```

```
        nn = (struct tree *) malloc(sizeof(struct tree));
```

```
        nn->left = NULL;
```

```
        nn->data = x;
```

```
        nn->right = NULL;
```

```
        if (root == NULL)
```

```
            root = nn;
```

```
        else
```

```
            insert(root, nn);
```

printf("\n do you wish to continue (y/n) ");

getchar();

ch = getchar();

getchar();

}

while(ch == 'y');

} // end of create function.

// inorder Traversal

void display(struct tree *temp)

{

if (temp != NULL)

{

display(temp->left);

printf("%c\n", temp->data);

display(temp->right);

}

}

void main()

{

create();

display(root);

}

(Adelson, Velski & Landis)

An AVL Tree is a binary search tree in which the difference of heights of left sub tree and right subtree for any node must be either $-1, 0, +1$.

inserting into AVL tree

Case (i) :- inserting a node into the left child of the left sub tree

(if tree unbalanced, use LL Rotation)

Case (ii) :- inserting a node into the right child of the left sub tree

(if tree unbalanced, use LR Rotation)

Case (iii) :- inserting a node into the right child of right sub tree

(if tree unbalanced,

use RR Rotation)

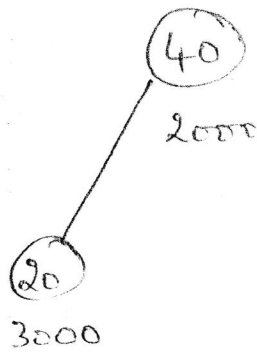
Case (iv) :- inserting a node into the left child of right subtree.

(if tree unbalanced,

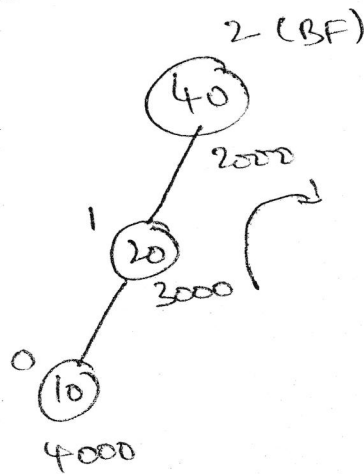
use RL Rotation)

Scenarios for LL Rotation

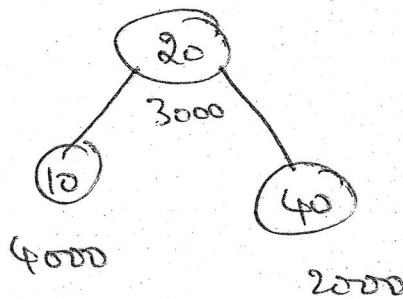
Ex 1 :-



Insert 10.

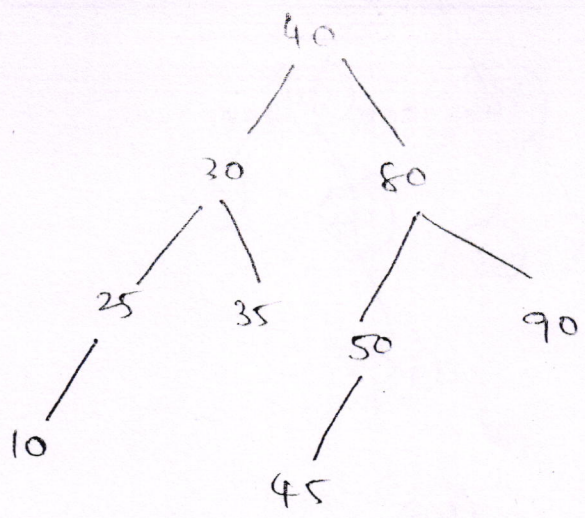


For the node at address 2000, the balance factor = 2 which is not accept \Rightarrow apply LL Rotation.
(ie Right Rotation)

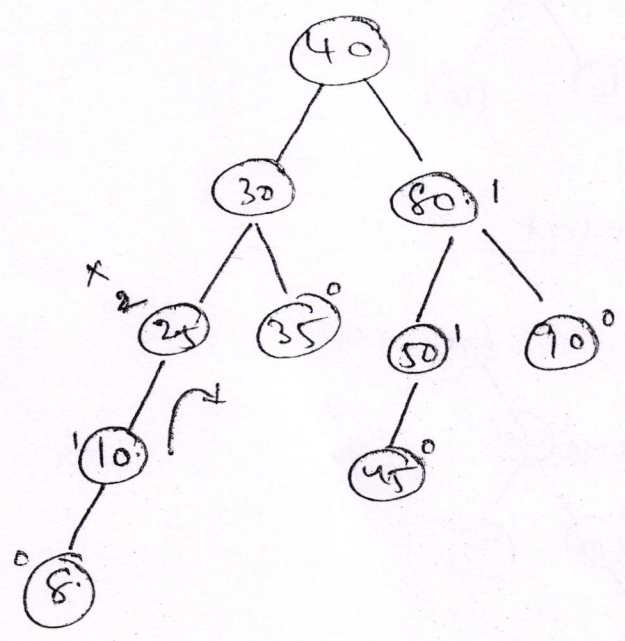


Ex 2

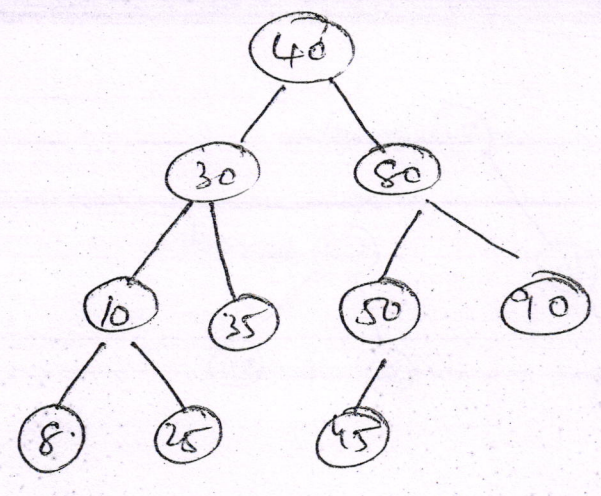
(4)



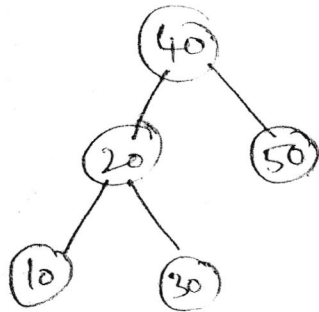
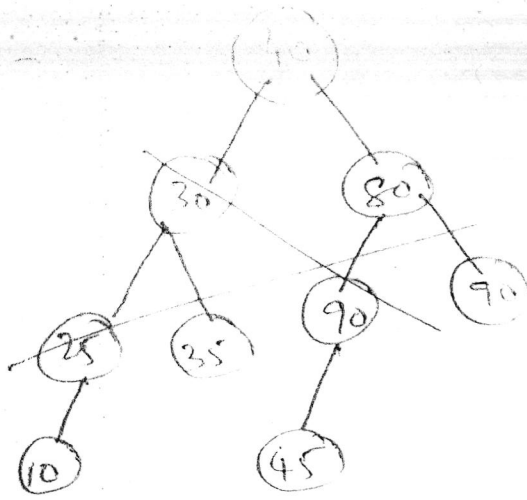
insert '8'



apply LL Rotation C



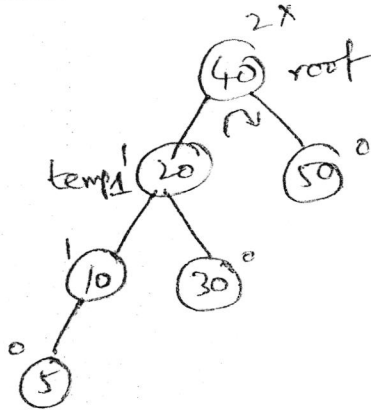
Ex 3



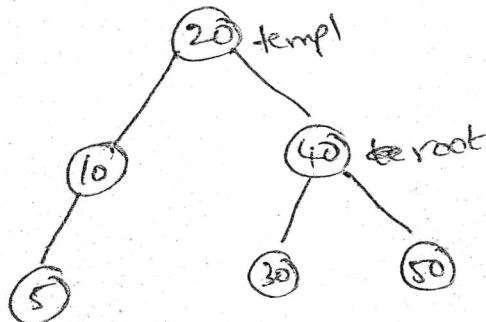
(a) insert 5

(b) insert 15

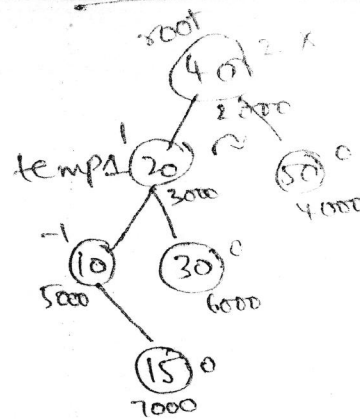
(a) insert 5



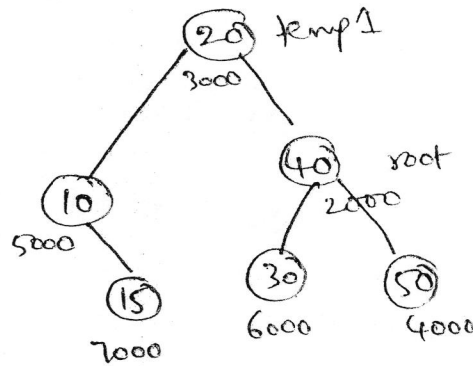
apply LL Rotation



(b) insert 15



apply LL Rotation.



Code for LL Rotation

temp1 = root → left

root → left = temp → right

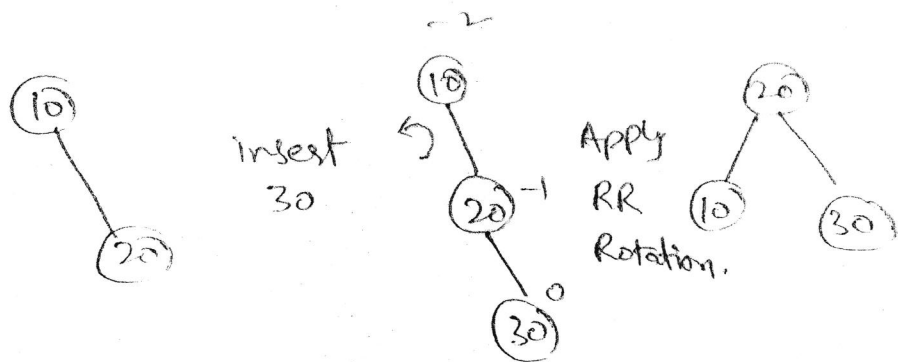
temp1 → right = root , root → BF = 0.

root = temp1

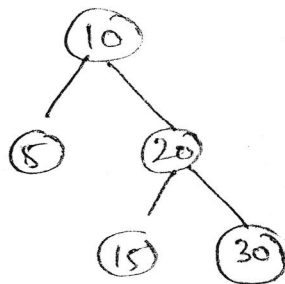
root → BF = 0.

Examples of RR Rotation

Ex 1

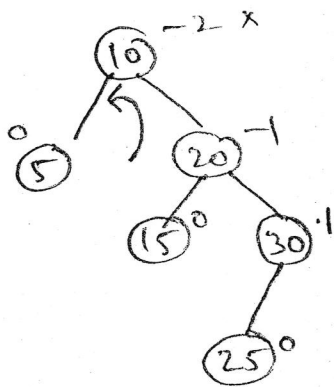


Ex 2

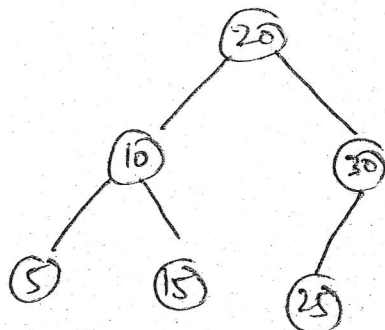


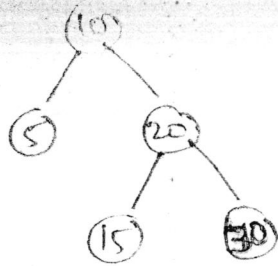
- (a) insert 25
- (b) insert 40

(a) insert 25

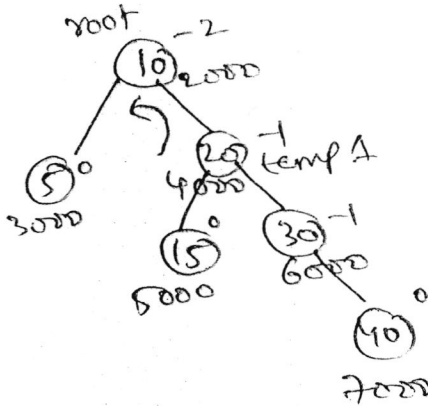


apply RR Rotation

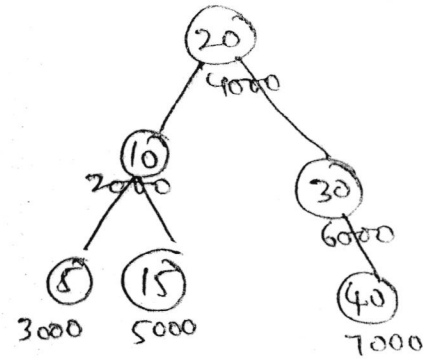




(b) Insert 40



apply
RR
Rotation



RR Rotation Code :-

temp1 = root → right;

root → right = temp1 → left;

temp1 → left = root;

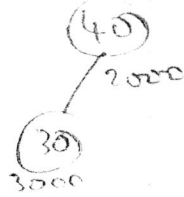
root → BF = 0;

root = temp1;

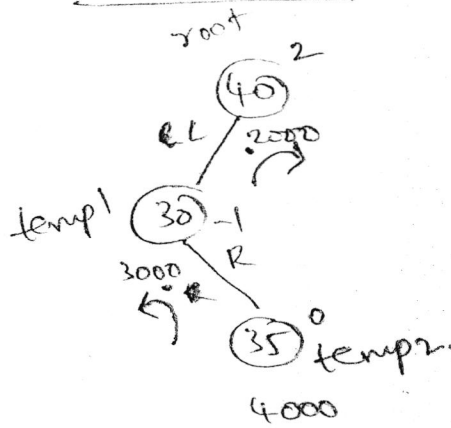
root → BF = 0;

Examples of LR Rotation

Ex1

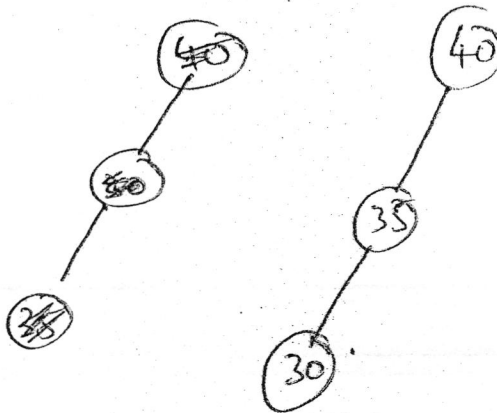


Insert 35.

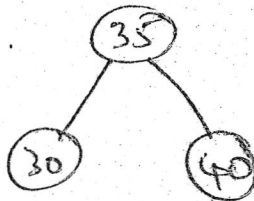


apply double Rotation. (LR)

step1 :- ~~apply~~

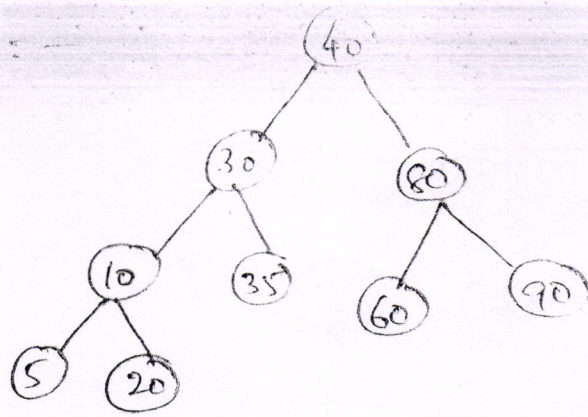


Step2



Ex 2 :-

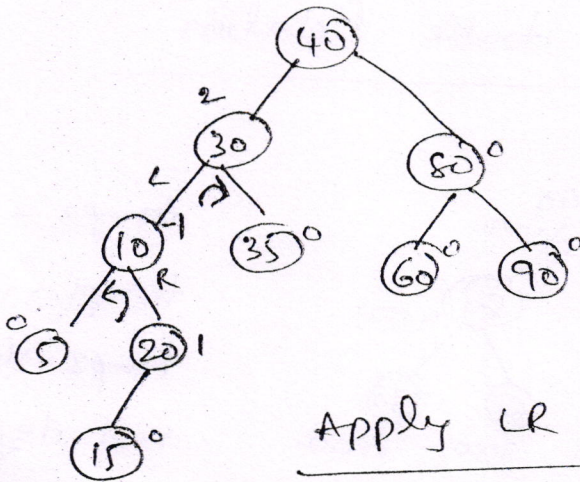
(7)



(a) insert 15

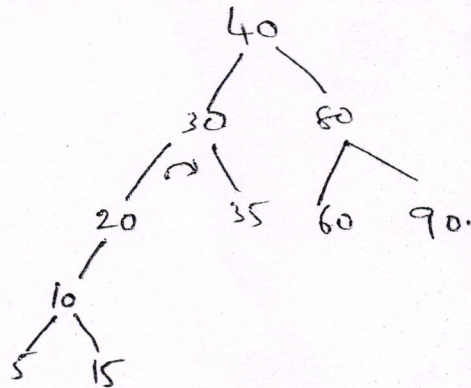
(b) insert 25

(a) insert 15

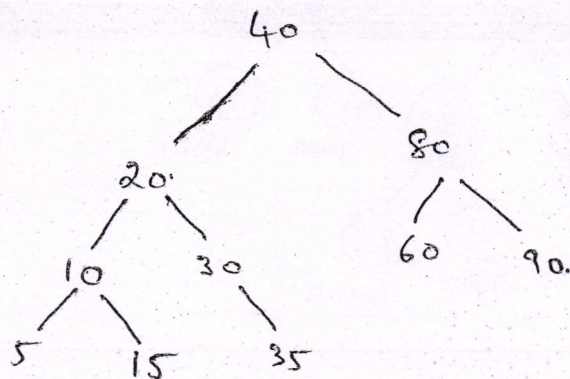


Apply LR Rotation

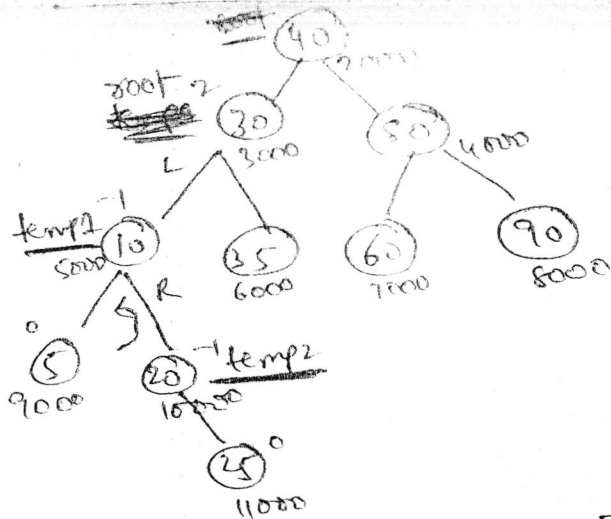
Step 1 :-



Step 2 :-



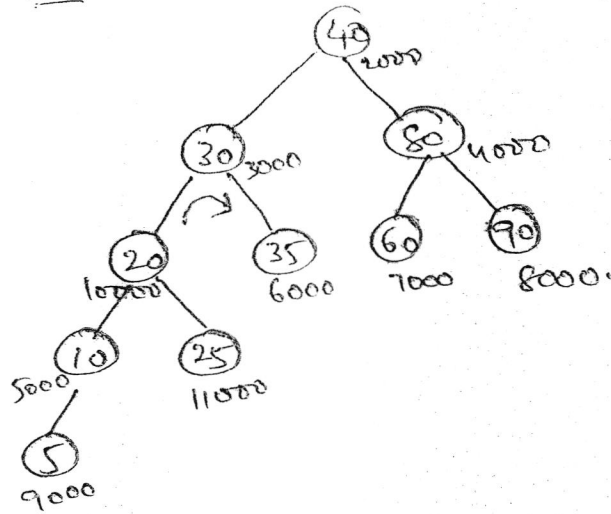
(1) Insertion



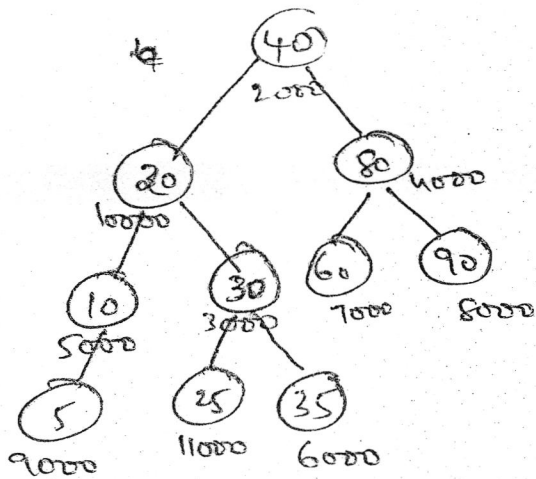
apply LR double Rotation

Code

Step1



Step2



temp2 = temp1 → right
 temp1 → right = temp2 → left
 temp2 → left = temp1
 root → left = temp2 → right
 temp2 → right = root;

{ if (temp2 → BF == 1)
 root → BF = -1;
 else
 root → BF = 0;

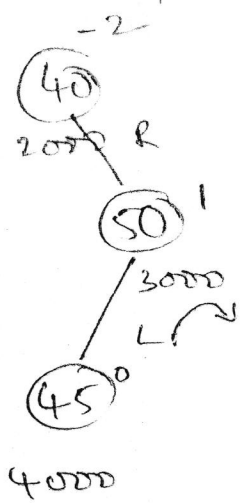
{ if (temp2 → BF == -1)
 temp1 → BF = 1;
 else
 temp1 → BF = 0;

root = temp2;

root → BF = 0.

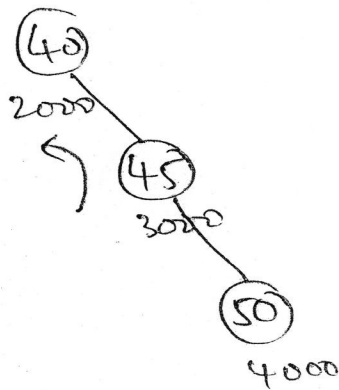
Example for RL Rotation :-

Ex 1 :-

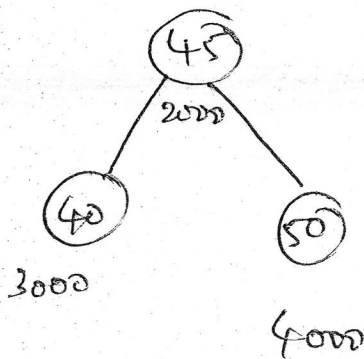


apply double Rotation.
(RL Rotation)

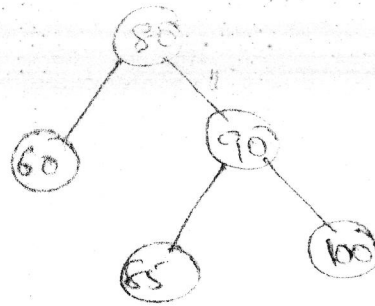
Step 1



Step 2



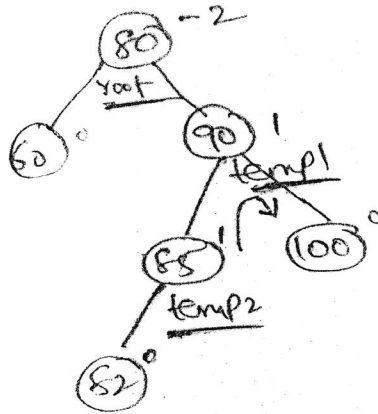
Ex 2



(a) Insert 82

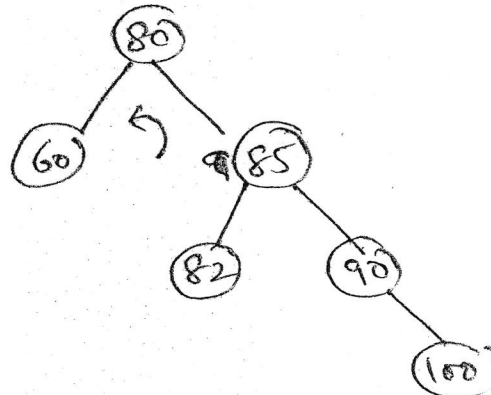
(b) Insert 86

(a) insert 82

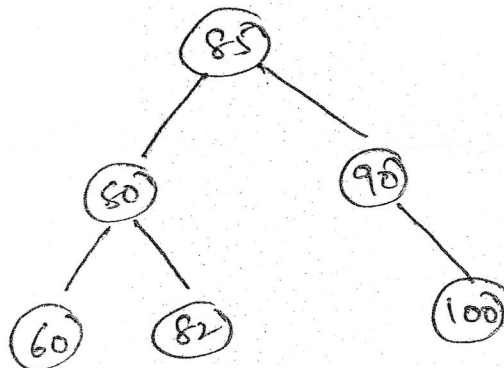


Apply RL Rotation (Rouble Rotation)

Step 1 :-



Step 2 :-



Code for RL Rotation

```

temp1 = root -> right
temp2 = temp1 -> left;
temp1 -> left = temp2 -> right;
temp2 -> right = temp1;
root -> right = temp2 -> left;
temp2 -> left = root;

```

```

if (temp2 -> BF == -1)
    root -> BF = 1;
else
    root -> BF = 0;

```

```

if (temp2 -> BF == 1)
    temp1 -> BF = -1;
else
    temp1 -> BF = 0;

```

```

root = temp2
root -> BF = 0;

```

Task 1 :-

Insert the following elements into the AVL Tree.

40, 30, 20, 60, 50, 80, 15, 28, 25.

Task 2 :-

Insert the following elements into the AVL Tree

A, V, L, T, R, E, I, S, O, K.

```
#include <stdio.h>
#include <stdlib.h>

struct avlnode
{
    struct avlnode *left;
    int data;
    int bf;
    struct avlnode *right;
};

typedef struct avlnode node;

node * root ;

node * insert ( node *root, int data, int *Current )
{
    node *temp1, *temp2;

    if ( root == NULL )
    {
        root = (node *) malloc ( sizeof (node) );

        root -> data = data;
        root -> left = NULL;
        root -> right = NULL;
        root -> bf = 0;

        *Current = 1;
        return root;
    }
}
```



```

if (data > root->data)
{
    root->right = insert(root->right, data, current);
    if (*current == 1)
    {
        switch (root->bf)
        {
            Case -1 : temp1 = root->right;
                if (temp1->bf == -1)
                {
                    printf("\n Single Rotation : RR\n");
                    root->right = temp1->left;
                    temp1->left = root;
                    root->bf = 0;
                    root = temp1;
                }
                else
                {
                    printf("\n double Rotation RL\n");
                    temp2 = temp1->left;
                    temp1->left = temp2->right;
                    temp2->right = temp1;
                    root->right = temp2->left;
                    temp2->left = root;

                    if (temp2->bf == -1)
                        root->bf = 1;
                    else
                        root->bf = 0;
                }
            }
        }
    }
}

```


if (temp2 → bf == 1)

root → bf = -1;

else

root → bf = 0;

if (temp2 → bf == -1)

temp1 → bf = 1;

else

temp1 → bf = 0;

root = temp2;

}

root → bf = 0;

* current = 0;

break;

Case 0 : root → bf = 1;

break;

Case -1 : root → bf = 0;

* current = 0;

}

}

}

(11)

```

if ( data > root->data )
{
    root->right = insert ( root->right, data, current );
    if ( *current == 1 )
    {
        switch ( root->bf )
        {
        case -1 : temp1 = root->right;
            if ( temp1->bf == -1 )
            {
                printf ( "\n Single Rotation : RR\n " );
                root->right = temp1->left;
                temp1->left = root;
                root->bf = 0;
                root = temp1;
            }
            else
            {
                printf ( "\n double Rotation RL\n " );
                temp2 = temp1->left;
                temp1->left = temp2->right;
                temp2->right = temp1;
                root->right = temp2->left;
                temp2->left = root;

                if ( temp2->bf == -1 )
                    root->bf = 1;
                else
                    root->bf = 0;
            }
        }
    }
}

```

```

if (temp2->bf == -1)
    temp1->bf = -1;
else
    temp1->bf = 0;

root = temp2;
}
root->bf = 0;
*Current = 0;
break;

```

```

Case 0 : root->bf = -1;
        break;

```

```

Case 1 : root->bf = 0;
        *Current = 0;

```

```

}
}
}
return root;
}

```

```

void display (node *temp)
{
    if (temp != NULL)
    {
        display (temp->left);
        printf ("\n %d", temp->data);
        display (temp->right);
    }
}

```

```
void main()
```

```
{
```

```
int current=1; int i, x;
```

```
root = NULL;
```

```
for (i=1; i<=15; i++)
```

```
{
```

```
printf("Enter data to insert ");
```

```
scanf("%d", &x);
```

```
root = insert(root, x, &current);
```

```
}
```

```
display(root);
```

```
}
```

Insert the following elements into the AVL Tree & Display in Inorder.

40, 50, 30, 60, 70, 45.

(i) insert 40

main()

{

root = NULL;

c = 1;

root = insert (NULL, 40, 5555); → goto (a)

c 1
5555 (Address)

↑ (b)

// root becomes 2000 after the call

}

(a) → insert (NULL, 40, 5555)

root = NULL

⇒ root = 2000 (create a new node
Let the address allocated is 2000)

2000 → data = 40

2000 → left = NULL

2000 → right = NULL.

2000 → BF = 0.

N | 40 | 0 | N
2000

c = 1

return 2000 → (b)

(ii) insert 50

main() {

2000 = insert(2000, 50, 5555); → (a)

}

(a) → insert(2000, 50, 5555)

(50 > 40) data > root → data

root → right = insert(root → right, data, c)

2000 → right = insert(NULL, 50, 5555) → (b)

(c) →

2000 → right = 3000

2000 → bf = 0 ⇒ Case 0 ∴ 2000 → bf = -1
break.

return 2000 → (d)

(b) → insert(NULL, 50, 5555)

root = NULL

create a newnode with addr '3000'

store data as 50, bf = 0, c = 1

return 3000 → (c)

40	-1
----	----

2000

50	0	1
----	---	---

3000

```

main()
{
  2000 = insert(2000, 30, 5555); → (a)
}
      ↑
      (d)

```

(a) → insert(2000, 30, 5555)

30 < 40 data < root → data

2000 → left = insert(2000 → left, 30, 5555) → (b)

← (c)

2000 → left = 4000

c = 1

2000 → bf = -1, ⇒ 2000 → bf = 0.

return 2000 → (d)

(b) → insert(NULL, 30, 5555)

root = NULL

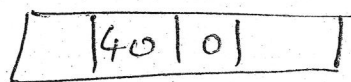
new node is created with addr 4000

30 stored as data

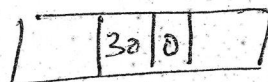
bf = 0

c = 1

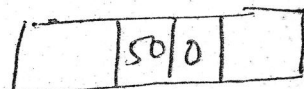
return 4000 → (c)



2000



4000



3000

(iv) insert 60

main()

```
{  
  2000 = insert(2000, 60, 5555); → (a)  
  } ← (f)
```

(a) → insert(2000, 60, 5555)

(60 > 40) data > root → data

2000 → right = insert(3000, 60, 5555) → (b)

← (e)

2000 → right = 3000

c=1, 2000 → bf = 0

Case 0 → 2000 → bf = -1,

return 2000 → (f)

(b) → insert(3000, 60, 5555)

(60 > 50) data > root → data

3000 → right = insert(3000 → right, 60, 5555) → (c)

← (d)

3000 → right = 5000

c=1, 3000 → bf = 0.

Case 0 → 3000 → bf = -1

return 3000 → (e)

(c) \rightarrow insert (NULL, 60, SSSS)

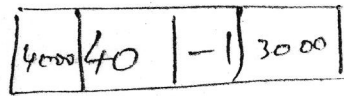
(15)

root = NULL

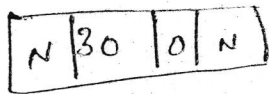
Creates a new node with addr 5000

Put data as 60, bf = 0, c = 1

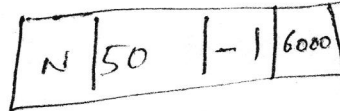
return 5000 \rightarrow b (d)



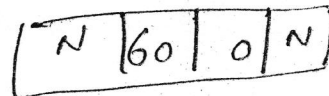
2000



4000



3000



6000

(v). insert 70

main()

```
{  
2000 = insert(2000, 70, 5555) → (a)  
}
```

↑ (h)

(a) → insert(2000, 70, 5555)

data > root → data

2000 → right = insert(3000, 70, 5555) → (b)

← (g)

2000 → right = 5000

c = 0, return 2000 → (h)

(b) → insert(3000, 70, 5555)

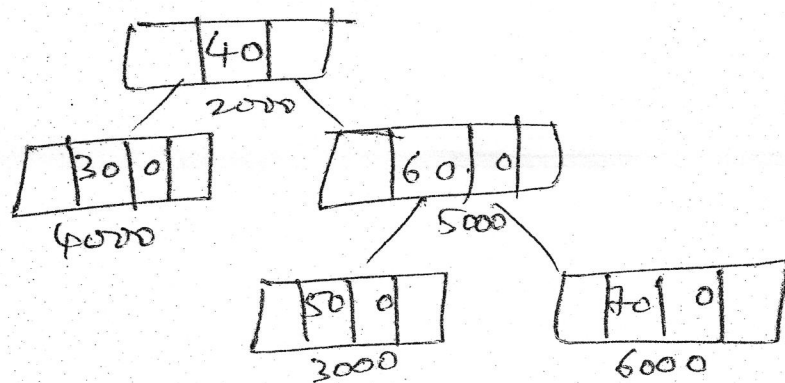
data > root → data.

3000 → right = insert(5000, 70, 5555) → (c)

← (f)

3000 → right = 5000, c = 1, 3000 → bf = -1

Case -1 ⇒ Right Rotation.



3000 → bf = 0

5000 → bf = 0 & root = 5000

return 5000 → (g)

(c) insert (5000, 10, 5555)

(16)

data > root → data (70 > 60)

5000 → right = insert (NULL, 70, 5555) → (d)
← (e)

5000 → right = 6000

c = 1

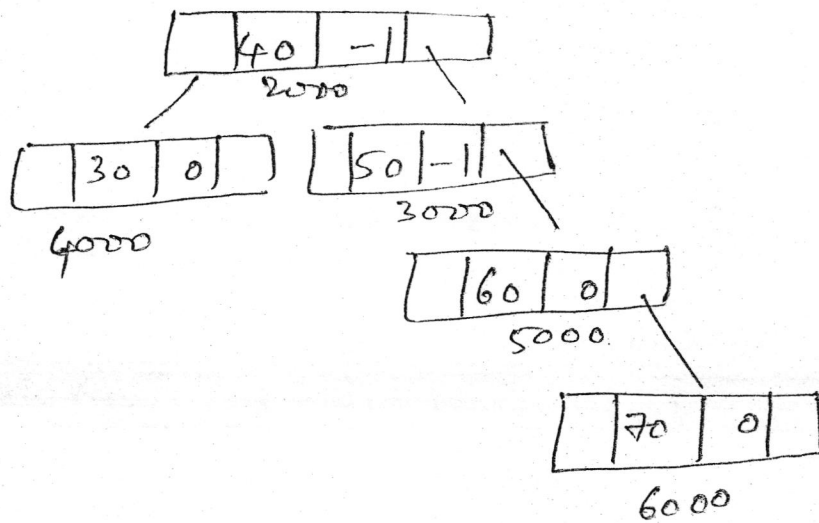
5000 → bf = 0

Case 0 ⇒ 5000 → bf = -1

return 5000 → (f)

(d) → insert (NULL, 70, 5555)

root = NULL, Create new node with address 6000
data as 70, bf = 0, c = 1.



return 6000 → (e)

(vi) insert 45

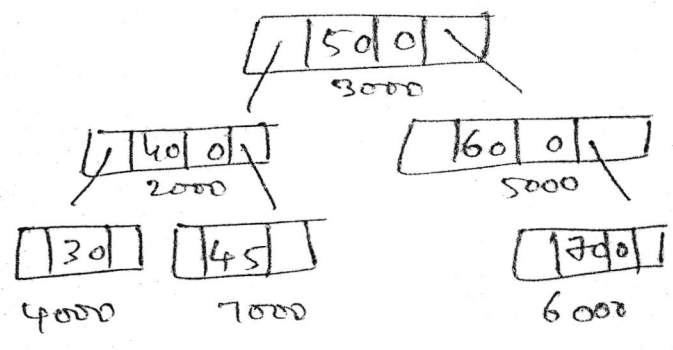
```
main()
{
  2000 = insert(2000, 45, 5555);  → (a)
}
↑ (h)
```

(a) insert(2000, 45, 5555)

(45 > 40) data > root → data

2000 → right = insert(5000, 45, 5555) → (b)
 ← (g)

c = 1, 2000 → bf = -1 ⇒ Case -1 (RL Rotation)



3000 → bf = 1 ⇒ 2000 → bf = 0, 5000 → bf = -1

root = temp2 = 3000, ⇒ 3000 → bf = 0.

c = 0, return 3000 → (h)

(b) → insert(5000, 45, 5555)

45 < 60

5000 → left = insert(3000, 45, 5555) → (c)

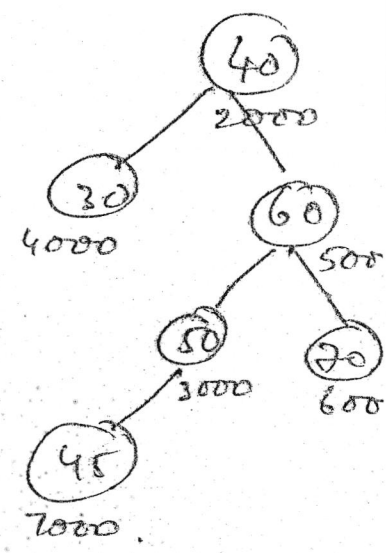
← (f)

5000 → left = 3000

c = 1, 5000 → bf = 0.

⇒ 5000 → bf = 1

return 5000 → (g)



(c) → insert(3000, 45, 5555)

45 < 50

3000 → left = insert(3000 → left, 45, 5555) → (d)

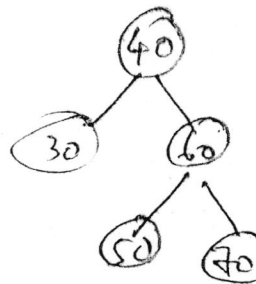
← (e)

3000 → left = 7000

c = 1

3000 → bf = 0 ⇒ 3000 → bf = 1

return 3000 → (f)



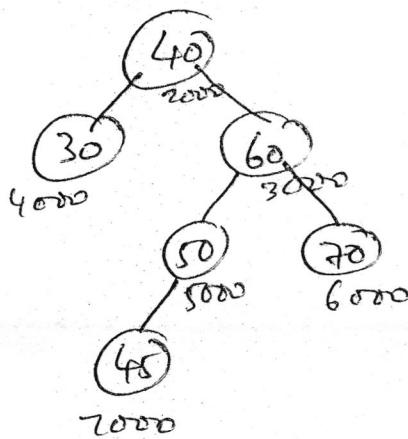
(d) → insert(NULL, 45, 5555)

root = NULL

Create a new node & let the address 7000

7000.

data as 45, bf = 0, c = 1



return 7000 → (e)

A B-tree of order m , is an m -way search tree with the following properties

- (i) Root must have atleast two children
- (ii) All the leaf nodes must be on the bottom level.
- (iii) All the leaf and internal nodes except leaf nodes must have atleast $\text{Ceil}(m/2)$ non empty children.
- (iv) if the node has ' n ' children, then it must have $n-1$ keys.

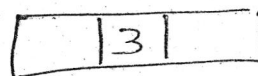
Task 1 :-

Insert the following values into the B-tree

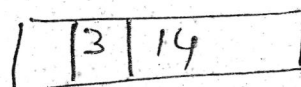
3, 14, 7, 1, 8, 5, 11, 17, 13, 6, 23, 12, 20, 26,
4, 16, 18, 24, 25, 19.

Solutions :-

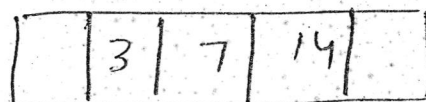
inserting 3



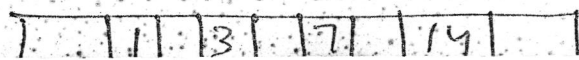
inserting 14



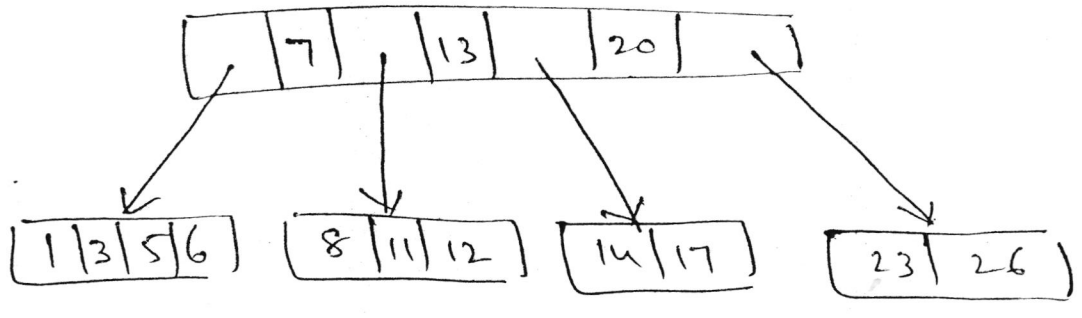
inserting 7



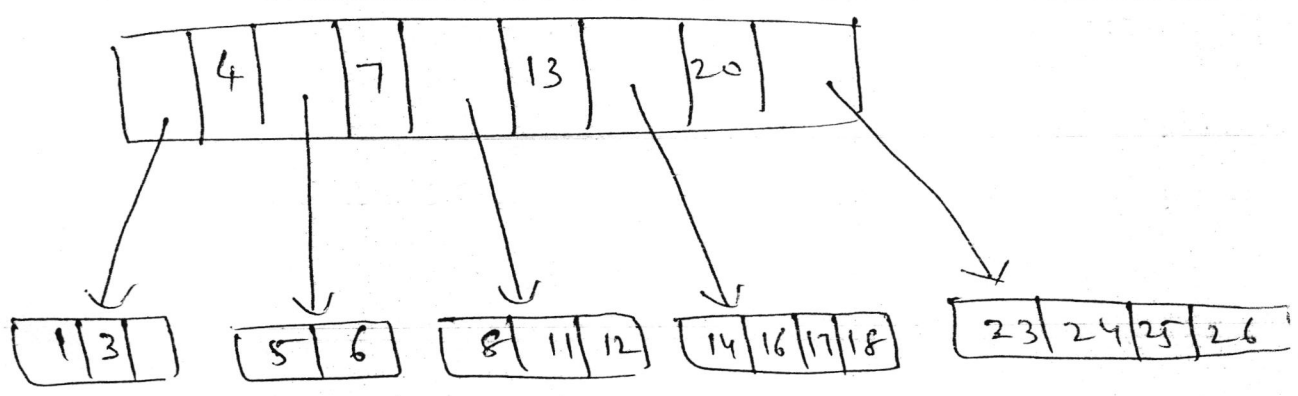
inserting 4



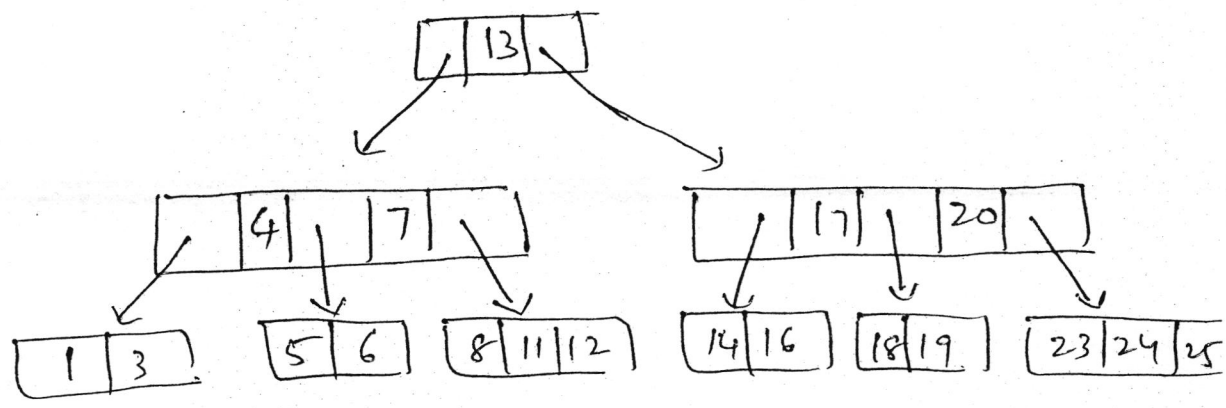
insert 26



insert 4



insert 19




```
#include <stdio.h>
#include <stdlib.h>
```

```
#define MAX 4
#define MIN 2
```

```
struct treenode
{
    int Count;
    int keys[MAX+1];
    struct treenode *links[MAX+1];
};
```

```
typedef struct treenode node;
```

```
int search(int, node *, int *);
```

```
void insertin(int, node *, node *, int);
```

```
node * insert(int, node *);
```

```
int move down(int, node *, int *, node **);
```

```
void split(int, node *, int node *, int,
           int *, node **);
```

```
void inorder(node *);
```

```

int search (int key, node *current, int *pos)
{
    if (key < current->keys[i])
    {
        *pos = 0;
        return 0;
    }
    else {
        for (*pos = current->count;
            key < current->keys[*pos] && *pos > 1;
            (*pos) --);

        if (key == current->keys[*pos])
            return 1;
        else
            return 0;
    }
}

```

```

void insertin (int med, node *medright, node *current,
              int pos)
{
    int i;
    for (i = current->count; i > pos; i--)
    {
        current->keys[i+1] = current->keys[i];
        current->links[i+1] = current->links[i];
    }
    current->keys[pos+1] = med;
    current->links[pos+1] = medright;

    current->count++;
}

```

(21)

```

node * insert (int x, node * temp)
{
    int medentry; node * medright, * newnode;
    if (move down (x, temp, & medentry, & medright))
    {
        newnode = (node *) malloc (sizeof (struct treenode));
        newnode -> count = 1;
        newnode -> keys [1] = medentry;
        newnode -> links [0] = temp;
        newnode -> links [1] = medright;
        return newnode;
    }
    return temp;
}

```

```

int move down (int x, node * current, int * med,
               node ** medright)
{
    int pos;
    if (current == NULL)
    {
        * med = x;
        * medright = NULL;
        return 1;
    }
    else
    {
        if (search (x, current, & pos))
            printf ("duplicate key");
        if (move down (x, current -> links [pos], med, medright))
        {
            if (current -> count < MAX)
            {
                insert in (* med, * medright, current, pos);
                return 0;
            }
            else {
                split (* med, * medright, current, pos, med, medright);
                return 1;
            }
        }
        return 0;
    }
}

```

```

void split (int med, node * medright, node * current,
            int pos, int * newmedian, node ** newright)
{
    int i;
    int median;

    if (pos <= MIN)
        median = MIN;
    else
        median = MIN + 1;

    *newright = (node *) malloc (sizeof (struct treenode));

    for (i = median + 1; i <= MAX; i++)
    {
        (*newright) -> keys [i - median] = current -> keys [i];
        (*newright) -> links [i - median] = current -> links [i];
    }

    (*newright) -> count = MAX - median;
    current -> count = median;

    if (pos <= MIN)
        insertIn (med, medright, current, pos);
    else
        insertIn (med, medright, *newright, pos - median);

    *newmedian = current -> keys [current -> count];
    (*newright) -> links [0] = current -> links [current -> count];
    current -> count --;
}

```

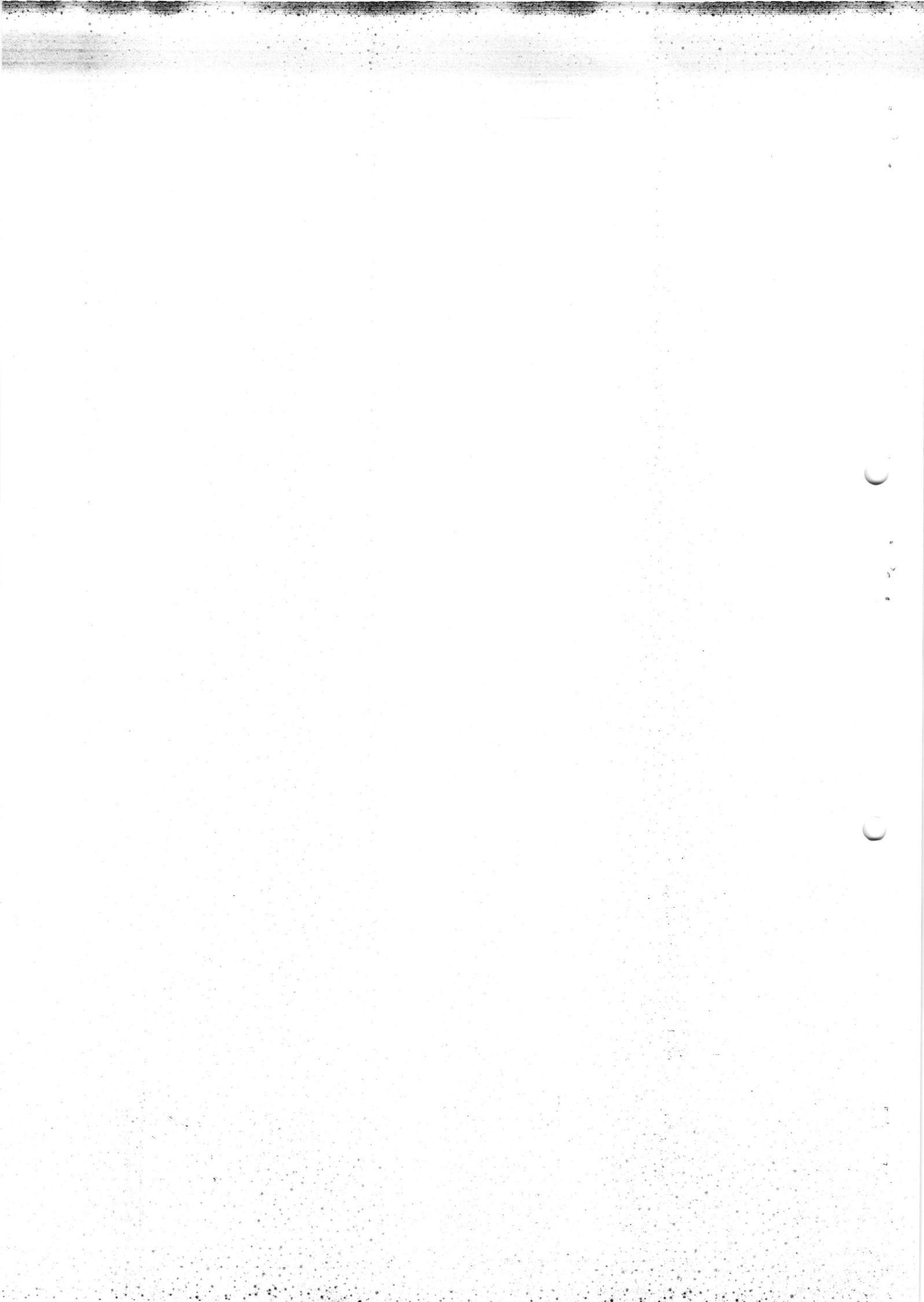
void inorder (node *temp)

```
{
    int pos;
    if (temp)
    {
        inorder (temp->links[0]);
        for (pos=1; pos <= temp->count; pos++)
        {
            printf ("%d", temp->keys[pos]);
            inorder (temp->links[pos]);
        }
    }
}
```

void main()

```
{
    node *root; int i, x;
    root = NULL;

    for (i=1; i <= 20; i++)
    {
        printf ("Enter the data to insert");
        scanf ("%d", &x);
        root = insert (x, root);
    }
    inorder (root);
}
```



(i) insert 3

```
main()
{
  node *root = NULL;
  root = insert(3, NULL) → (a)
}
      ↑
      (d)
```

(a) → insert(3, NULL)

if (movedown(3, NULL, &me, &mr)) → (b)

← (c)

Creates new node, let the address = 2000

newnode → ^{Keys}~~entry~~[i] = me = 3

newnode → link[0] = root = NULL

newnode → link[1] = mr = NULL

return 2000 → (d)

(b) → move down(3, NULL, &me, &mr)

cur = NULL

me = x

mr = NULL

return 1 → (c)

	3			
NULL	NULL			

2000

(11) insert

main()

root = insert(14, 2000) → (a)
↑ (h)

(a) → insert(14, 2000)

if (movedown(14, 2000, &me, &mr)) → (b)

← (g)
return 2000 → (h)

(b) → movedown(14, 2000, &me, &mr)

cur = NULL

Search (14, 2000, &pos) ⇒ pos = 1

if (move down(14, 2000 → link[i], me, mr);

← (d) → (c)

2000 → Count < MAX Then

insertIn(14, NULL, 2000, 1) → (e)

← (f)

return 0 → (g)

(c) → movedown(14, NULL, me, mr)

cur == NULL me = 14 mr = NULL return 1 → (d)

(e) → insert in(14, NULL, 2000, 1)

places 14 as 2nd key & link[2] = NULL, Count++

2				
	3	14		
N	N	N		

return ; → (f)

main()

{
root = insert(1, 2000) → (a)
}

~~insert~~ (a) → insert(7, 2000)

if (movedown(7, 2000, &me, &mr)) → (b)
← (g)

return 2000 → (h)

(b) → move down(7, 2000, &me, &mr)

cur = NULL search(7, 2000, &pos) → pos = 1

if (movedown(7, 2000 → link[1], me, mr)) → (c)
← (d)

2000 → cout < MAX then

insertin(7, N, 2000, 1) → (e)

← (f)

return 0 → (g)

(c) → move down(7, NULL, me, mr)

cur = NULL, me = 7, mr = NULL, return 1 → (d)

(e) → insertin(7, NULL, 2000, 1)

move 2000 → link[2], 2000 → key[2] to right

place 2000 → key[2] = 7, 2000 → link[2] = NULL.

3				
	3	7	14	
N	N	N	N	

return ; → (f)

(iv) insert 1

o/p

4				
	1	3	7	14
N	N	N	N	N

main()

```
{  
  root = insert(8, 2000) → (a)  
  ← (j)  
}
```

(a) → insert(8, 2000)

if (movedown(8, 2000, &me, &mr)) → (b)
← (i)

Creates new node, let the address is 4000, Count = 1

4000 → ~~key~~ Key[1] = 7, 4000 → links[0] = 2000,

4000 → links[1] = mr = 3000, return 4000 → (j)

(b) → movedown(8, 2000, &me, &mr)

CUR = NULL, search(8, 2000, &pos) → pos = 3

if (movedown(8, 2000 → link[3], me, mr)) → (c)
← (d)

2000 → Count < MAX false split(8, NULL, 2000, 3, me, mr) → (e)
← (h)

return 1 → (i)

(c) → movedown(8, NULL, me, mr)

CUR = NULL, me = 8, mr = NULL, return 1 → (d)

~~split~~ (e) → split(8, NULL, 2000, 3, me, mr)

pos < MIN, false ⇒ median = 3

newright = new node (let the addr is 3000)

move entries after median to newright (ie 3000)

newright → Count = 1

2000 → Count = 3

pos < MIN false

insertin(8, NULL, 3000, pos - median) → (f)

newmedian = cur->entry [cur->count]

3000 → link[0] - 2000 → link[3] = NULL

2000 → count = 1 ; 2000 → count = 2

updates :- me = 7

nr = 3000

return ; → (h)

insertin(8, NULL, 3000, 0)

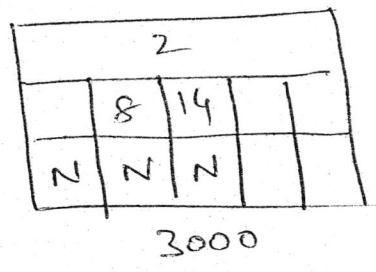
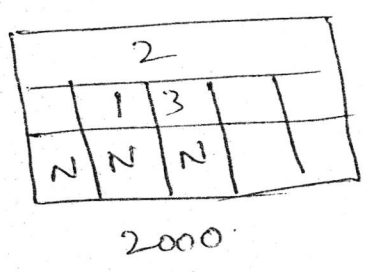
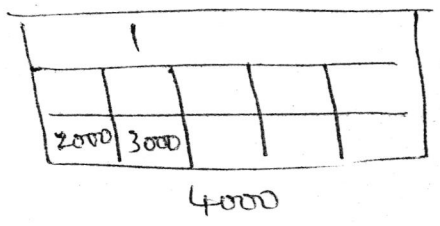
move 3000 → key[1]

3000 → link[1] to right

*

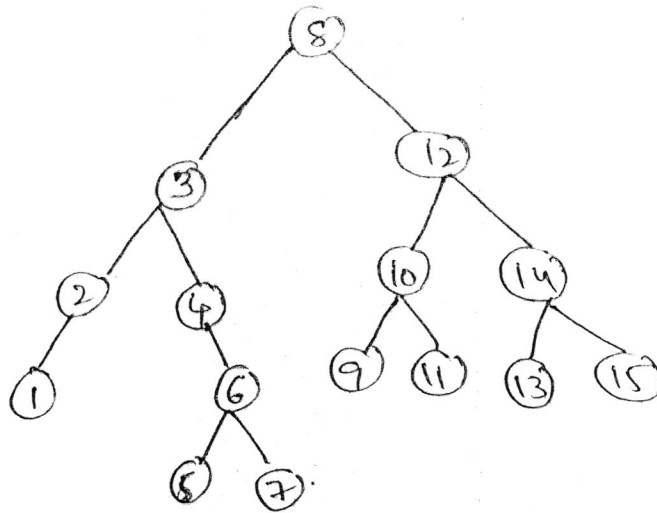
store 3000 → key[1] = 8

3000 → link[1] = NULL



return ; → (g)

Node 3, Parent, grand parent involved in splay operation indicate zig-zag (LR rotation)



To bring '3' to Root, we need Zig (L Rotation)

